



# Strictly Local Patterns are not Closed Under Optimization

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# Introduction

- In Optimality Theory (Prince & Smolensky 1993), optimization over strictly local (McNaughton & Papert 1971) constraints can generate fully regular patterns
- Take SL to be the *Constraint Definition Language* (Eisner 1997b; Potts & Pullum 2002; de Lacy 2011) (CDL) for markedness constraints
- SL constraints bans on contiguous substructure: PARSE –  $\neg\check{\sigma}$

# Introduction

- Set of markedness-only stress constraints produces novel “sour grapes”-like stress pattern, importantly not SL
- Tells us that establishing a CDL is no guarantee of a typology with matching complexity

# Roadmap

- Introduce the constraint set
- Explore the sour grapes pattern in detail
- Prove that the pattern is properly regular
- Discuss implications and future work

# Questions

- When formally evaluating OT, some questions we can ask:
  - What is the complexity level of the CON constraints? (Eisner 1997c; Potts & Pullum 2002; Jardine & Heinz 2016)
  - What is the nature of the functions that can be described by OT grammars? (Eisner 1997a; Frank & Satta 1998; Riggle 2004; Buccola 2013); and:
  - Examine the outputs of these functions as *phonotactic* patterns: as formal languages.

# GEN

- Consider strings of syllables – unstressed  $\sigma$ , stressed  $\acute{\sigma}$ , unparsed  $\check{\sigma}$ , and foot boundaries right  $)$ , and left  $($
- $(\acute{\sigma}\sigma)\check{\sigma}\check{\sigma}\check{\sigma}$  or  $(\acute{\sigma}\sigma)(\acute{\sigma}\sigma)(\acute{\sigma}\sigma)$
- No superbinary feet (this requirement is SL)
- Allow stressless strings; obligatoriness (requiring at least one stress) Locally Testable; Rogers et al. (2013)

# Constraints

- SL class definable with *conjunctions of negative literals* (CNLs), where literals are substructure:  $\neg s_1 \wedge \neg s_2 \wedge \dots \wedge s_n$
- Statements forbidding contiguous substructures, no requirement of structure
- Relevant to markedness constraints in OT, overwhelmingly negative i.e. ban certain structures
- Example: TROCH, bans iambs and unary feet  $\neg(\sigma\acute{\sigma}) \wedge \neg(\acute{\sigma})$

# Constraints

- Strong prediction that markedness constraints are local only
- Banishes more complex constraints from CON
- ALIGN-type constraints (McCarthy & Prince 1993); more powerful, produce pathological patterns (Eisner 1997b; Hyde 2012)



# Constraints

- Defined with CNL logic
- Count number of violations – number of ill-formed structures
- TROCH:  $\neg (\sigma\acute{\sigma}) \wedge \neg (\acute{\sigma})$ 
  - Violated by strings  $\check{\sigma}(\sigma\acute{\sigma})$  and  $(\acute{\sigma})(\sigma\acute{\sigma})$
  - Unviolated by strings  $\check{\sigma}\check{\sigma}(\acute{\sigma}\sigma)$  and  $(\acute{\sigma}\sigma)(\acute{\sigma}\sigma)$
- Defined over alphabet  $\Sigma = \{(\,), \sigma, \acute{\sigma}, \check{\sigma}\}$

# Constraints

Constraint set:

IAMB violated by trochees and unary feet;  $\neg (\acute{\sigma}\sigma) \wedge \neg (\acute{\sigma})$

TROCHEE violated by iambs and unary feet;  $\neg (\sigma\acute{\sigma}) \wedge \neg (\acute{\sigma})$

PARSE violated by an unparsed syllable;  $\neg \check{\sigma}$

\* $\check{\sigma}F$ ;  $\neg \check{\sigma}(\sigma \wedge \neg \check{\sigma}(\acute{\sigma}$

\* $F\check{\sigma}$ ;  $\neg \sigma)\check{\sigma} \wedge \neg \acute{\sigma})\check{\sigma}$

# Constraints

- $*\check{\sigma}F$  and  $*F\check{\sigma}$   
 $\neg\check{\sigma}(\sigma \wedge \neg\check{\sigma}(\acute{\sigma}))$  and  $\neg\sigma)\check{\sigma} \wedge \neg\acute{\sigma})\check{\sigma}$

$*\check{\sigma}F$			$*F\check{\sigma}$	
$(\acute{\sigma}\sigma)\check{\sigma}(\acute{\sigma}\sigma)$	$(\acute{\sigma}\sigma)(\acute{\sigma}\sigma)$		$(\acute{\sigma}\sigma)\check{\sigma}(\acute{\sigma}\sigma)$	$\check{\sigma}(\acute{\sigma}\sigma)$
$\check{\sigma}(\acute{\sigma}\sigma)\check{\sigma}(\acute{\sigma}\sigma)$	$(\acute{\sigma}\sigma)(\acute{\sigma}\sigma)\check{\sigma}$		$(\acute{\sigma}\sigma)\check{\sigma}$	$(\acute{\sigma}\sigma)(\acute{\sigma}\sigma)$

- Motivate placement of feet
- Similar to  $*Ft/_\sigma$  and  $*Ft/\sigma_$  discussed in McCarthy (2003); defined as CNLs

# Constraints

- Troch  $\neg (\sigma\acute{\sigma}) \wedge \neg (\acute{\sigma})$  and Iamb  $\neg (\acute{\sigma}\sigma) \wedge \neg (\acute{\sigma})$

TROCH		IAMB	
$(\acute{\sigma}\sigma)(\sigma\acute{\sigma})$	$(\acute{\sigma}\sigma)(\acute{\sigma}\sigma)$	$(\acute{\sigma}\sigma)(\sigma\acute{\sigma})$	$\acute{\sigma}(\sigma\acute{\sigma})$
$(\sigma\acute{\sigma})(\acute{\sigma})$	$(\acute{\sigma}\sigma)$	$(\acute{\sigma}\sigma)(\acute{\sigma})$	$(\sigma\acute{\sigma})(\sigma\acute{\sigma})$

# Constraints

- PARSE: constraint against unparsed syllables  
     $\neg \check{\sigma}$

PARSE

$(\acute{\sigma}\sigma)\check{\sigma}$        $(\acute{\sigma}\sigma)$

$(\acute{\sigma}\sigma)\check{\sigma}\check{\sigma}$        $(\acute{\sigma}\sigma)(\acute{\sigma}\sigma)$

$(\acute{\sigma}\sigma)\check{\sigma}\check{\sigma}\check{\sigma}$        $(\acute{\sigma}\sigma)(\acute{\sigma}\sigma)(\acute{\sigma})$

# Constraints

- All constraints from the literature with an explicit CNL definition
- Application of constraints consistent with use in literature

# Typology

- Analysis in OTWorkplace (Prince et al. 2007-2017) reveals typology of 9 languages: 2 sour grapes languages, 1 stressless language, 2 ambiguous languages (more than one optimal output), 4 near-misses of attested patterns (iterating binary feet)

# Sour Grapes Stress

- Sour grapes phenomena in harmony, spreading, and tone (Padgett 1995; Wilson 2003, 2006; McCarthy 2010; Jardine 2016)
- If some feature cannot spread completely, candidate with no spreading wins instead
- Canonically involves markedness-faithfulness interaction (AGREE vs. IDENTIO(F))
- Here there are only CNL markedness constraints



# Sour Grapes Stress

σ̄

(σ̄σ)

σ̄σ̄σ̄

(σ̄σ)(σ̄σ)

σ̄σ̄σ̄σ̄σ̄

(σ̄σ)(σ̄σ)(σ̄σ)

σ̄σ̄σ̄σ̄σ̄σ̄σ̄

...

- Want to build binary feet to the end; if this can't be done, build no feet instead. No “spread” of feet in odd-syllable forms
- Pathological – no such extreme sensitivity to word length in natural language stress patterns

# Sour Grapes Stress

ǒ

(óσ)

ǒǒǒ

(óσ)(óσ)

ǒǒǒǒǒ

(óσ)(óσ)(óσ)

ǒǒǒǒǒǒǒ

...

input	winner	loser	*σF	*Fσ	TROCH	PARSE	IAMB
3syll	ǒǒǒ	ǒ(óσ)	W			L	W
3syll	ǒǒǒ	(σó)ǒ		W		L	W
1syll	ǒ	(ó)			W	L	W
2syll	(óσ)	ǒǒ				W	L

# Sour Grapes Stress

$\check{\sigma}$

$(\acute{\sigma}\sigma)$

$\check{\sigma}\check{\sigma}\check{\sigma}$

$(\acute{\sigma}\sigma)(\acute{\sigma}\sigma)$

$\check{\sigma}\check{\sigma}\check{\sigma}\check{\sigma}\check{\sigma}$

$(\acute{\sigma}\sigma)(\acute{\sigma}\sigma)(\acute{\sigma}\sigma)$

$\check{\sigma}\check{\sigma}\check{\sigma}\check{\sigma}\check{\sigma}\check{\sigma}$

...

input	winner	loser	$*_{\sigma}F$	$*F_{\sigma}$	TROCH	PARSE	IAMB
3syll	$\check{\sigma}\check{\sigma}\check{\sigma}$	$\check{\sigma}(\acute{\sigma}\sigma)$	W			L	W
3syll	$\check{\sigma}\check{\sigma}\check{\sigma}$	$(\sigma\acute{\sigma})\check{\sigma}$		W		L	W
1syll	$\check{\sigma}$	$(\acute{\sigma})$			W	L	W
2syll	$(\acute{\sigma}\sigma)$	$\check{\sigma}\check{\sigma}$				W	L

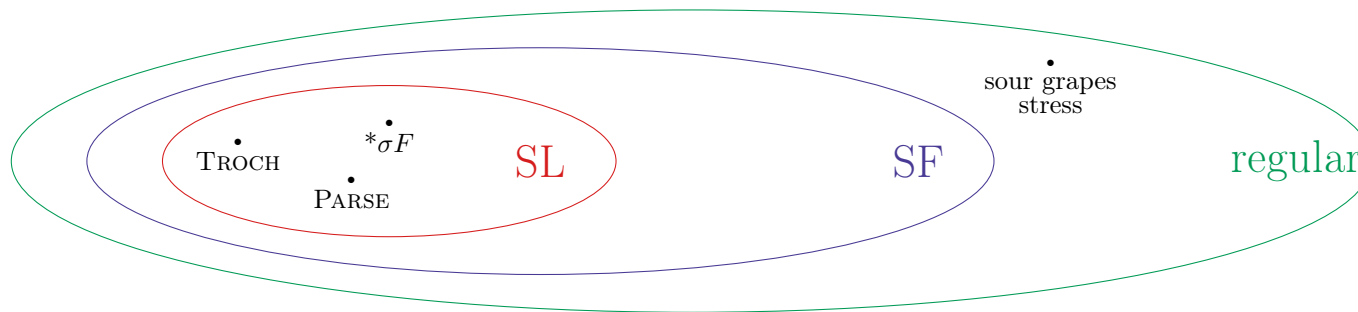
- In odd-syllable forms, cannot satisfy  $*_{\check{\sigma}}F$  or  $*F_{\check{\sigma}}$  with binary feet
- Any unary feet violate TROCH
- In even syllable forms, full satisfaction of PARSE – anything less incurs violations of higher ranked constraints

# Sour Grapes Stress

- Sour grapes-like stress pattern from markedness constraints only
- Generated by SL constraints, pattern is properly regular
- SL patterns are not closed under optimization

# Star Free?

- Sour grapes pattern discussed here is regular (see Appendix); can also show is not Star Free (McNaughton & Papert 1971, (SF))
- Natural language stress patterns overwhelmingly SF (Heinz 2009; Rogers et al. 2013)
- SF higher-level complexity class than SL, supports claim of lack of closure under optimization



# Not Star Free

- Alphabet change:  $\Sigma = \{(\, , \, \sigma\}$
- Before distinguished between stressed, unstressed, unparsed syllables – important in generating specific pattern, not necessary for studying its general properties

# Not Star Free

- Sour grapes-like language as a stringset:

$$L = \{\sigma$$

$$(\sigma\sigma)$$

$$\sigma\sigma\sigma$$

$$(\sigma\sigma)(\sigma\sigma)$$

$$\sigma\sigma\sigma\sigma\sigma$$

$$(\sigma\sigma)(\sigma\sigma)(\sigma\sigma)$$

$$\sigma\sigma\sigma\sigma\sigma\sigma\sigma\dots\}$$

- This  $L$  is not star free

# Not Star Free

**Theorem 1** (McNaughton & Papert 1971) A language  $L$  is Star-Free iff it is non-counting, that is, iff there exists some  $n > 0$  such that for all strings  $u, v, w$  over  $\Sigma$ , if  $uv^n w$  occurs in  $L$  then  $uv^{n+i}w$ , for all  $i \geq 1$ , occurs in  $L$  as well.

- $\exists n \forall i$  such that  $uv^n w \in L \rightarrow uv^{n+i}w \in L$
- Find two classes of counter-examples – one for odd  $n$  and one for even  $n$  and show that any even or odd number  $n$  (any integer) will fail the requirements of the theorem
- Prove that the sour grapes pattern is fully regular
- No string  $\sigma\sigma\sigma^n$  for even  $n$ , can use as target for  $uv^{n+i}w$



# Not Star Free

Odd  $n$ ,  $i = 1$ ,  $v = \sigma$

$$\begin{array}{ccc} uv^n w \in L & \rightarrow & uv^{n+i} w \in L \\ n & & \\ 1 & \sigma\sigma\sigma\sigma & \sigma\sigma\sigma\sigma\sigma \notin L \\ 3 & \sigma\sigma\sigma\sigma\sigma\sigma & \sigma\sigma\sigma\sigma\sigma\sigma\sigma \notin L \\ 5 & \sigma\sigma\sigma\sigma\sigma\sigma\sigma\sigma & \sigma\sigma\sigma\sigma\sigma\sigma\sigma\sigma\sigma \notin L \\ & & \vdots \end{array}$$

- Can construct same argument for even  $n$  (see Appendix)

# Not Star Free

- It is not the case that for all  $i \geq 1$ , there is an odd  $n$  or even  $n$  such that if  $uv^n w$  is a string of  $L$  then  $uv^{n+i} w$  is a string of  $L$  for all  $i \geq 1$
- Proves that Thm. 1 does not hold for the sour grapes-style pattern
- Proves that this pattern is not SF and so is properly regular

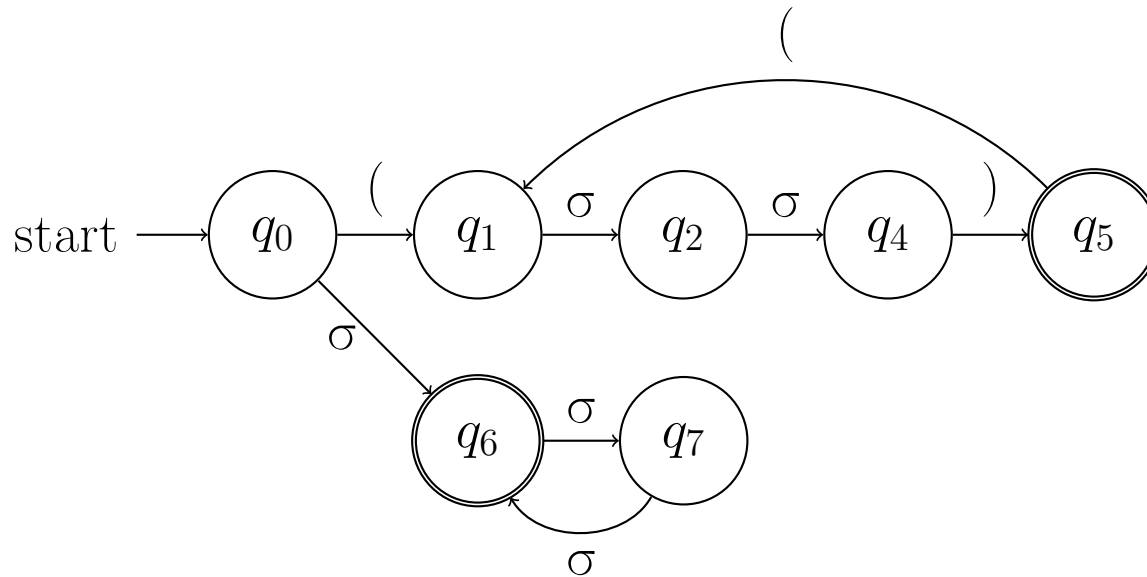
# Discussion

- A system of SL constraints that produced a fully regular pattern
- Pattern was a novel sour grapes-type pattern in stress
- What happens with strictly piecewise constraints? Still CNL logic but adds precedence (non-local)
  - ALIGN-type constraints? Is e.g.  $\text{ALIGN}(F,R,Pwd,R,\sigma)$  writeable as SP constraint  $\neg )\dots\sigma\dots]_{\omega}$  and does this produce things like the *Midpoint Pathology* (Eisner 1997b; Hyde 2012)
- What is the typology of CDLs with other levels of logic?

# Thanks!

Thanks to all viewers and all involved in production, particularly Adam Jardine and Bruce Tesar.

# Appendix: Regularity



- Top path – only accepting state after a binary foot has been read
- Bottom path – only accepting state after an odd number of syllables and no foot boundaries have been read

# Appendix: Not Star Free, Even $n$

Even  $n$ ,  $i = 1$ ,  $v = \sigma$

$$\begin{array}{ccc} uv^n w \in L & \rightarrow & uv^{n+i} w \in L \\ n & & \\ 2 & \sigma\sigma\sigma\sigma & \sigma\sigma\sigma\sigma\sigma \notin L \\ 4 & \sigma\sigma\sigma\sigma\sigma\sigma & \sigma\sigma\sigma\sigma\sigma\sigma\sigma \notin L \\ 6 & \sigma\sigma\sigma\sigma\sigma\sigma\sigma\sigma & \sigma\sigma\sigma\sigma\sigma\sigma\sigma\sigma\sigma \notin L \\ & & \vdots \end{array}$$

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